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$$\begin{split} T1! T+/)B\$! &(63)! ?55?! : F''! \&\%\%\#) ; \$'! \&!=\$+1 '! \&G\$1 'G\$1/!/)!/-\$! Y \&/\$\# WQ\&80/C! \\ 2\$\#/0(0+\&/0) 1I!!] -0=!\&G\$1 'G\$1/!9\#\&1/\$'!\%\$\#G0==0) 1!/)! '0=+-\&\#9\$!/\#\&/\$'!E\&/\$\#!/)!\&! \\ =\$+1 '!=/)\#G! E\&/\$\#!B\&=01>!<\&=01!?[>!) 18C!0(!<\&=01!?:!B\$+\&G\$!(088\$'!/)!+\&\%\&+0/CI!] -\$!\&G\$1 'G\$1/!\&\&)!9\#\&1/\$'!\&\%\%\#) ; \&8!/)! '0=+-\&\#9\$!=/\&1 '019!=Q\#(\&+\$!E\&/\$\#!01!/-\$!) \\ \%) 1 '!/)!/-\$!)Q/(\&88!)(!<\&=01!?:!E0/-)Q/!/\#\&/G\$1/>!&=!8) 19!\&=!/-\$!E\&/\$\#!E\&=!1)/!01! \\ +) 1/\&+/!E0/-!\%)/\$1/0\&&8C!+1 1/\&G01\&/\$'!=\$'0G\$1/c! \end{split}$$

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:F"!	: \$%&#/G\$1/!)(!F1;0#)1G\$1/&8!"#)/\$+/0)1!</td></tr><tr><td>F`[!</td><td>F1;0#)1G\$1/&8!`)/0(0+&/0)1![)#G!</td></tr><tr><td>FTFJ!</td><td>$F \ = \frac{1}{100} (0+1)(!F1;0) = \frac{1}{100} (0.000) = \frac{1}{100} (0.0000) = \frac{1}{100} (0.00000) = \frac{1}{100} (0.000000) = \frac{1}{100} (0.0000000) = \frac{1}{100} (0.0000000) = \frac{1}{100} (0.000000) = \frac{1}{100} (0.00000) = \frac{1}{100} (0.00000) = \frac{1}{100} (0.000000) = \frac{1}{100} (0.00000) = \frac{1}{100} (0.000000) = \frac{1}{100} (0.000000) = \frac{1}{100} (0.00000) = \frac{1}{1$</td></tr><tr><td>F" J !</td><td>F1;0#)1G\$1/&8!"#)/\$+/0)1!J9\$1+C!</td></tr><tr><td>F"2!</td><td>F\%)=Q#\$!")01/!2)1+\$1/#&/0)1!</td></tr><tr><td>F"b!</td><td>F / #& + / & B8 ! " /#) 8 QG! bC' #) + & #B) 1 = !</td></tr><tr><td>F7.!</td><td>F((\$+/=!7&19\$K.\$'0&1!</td></tr><tr><td>b J D"!</td><td>b \$&8/-!&1 '!D&(\$/C!''8&1!</td></tr><tr><td>H7J!</td><td>HGG\$'0&/\$!7\$=%)1=\$!J+/0)1!</td></tr><tr><td>*D"!</td><td>*0+\$1=\$'!D0/\$!"#)(\$==0)1&8!</td></tr><tr><td>. `J!</td><td>.)10/)#\$'!`&/Q#&8!J//\$1Q&/0)1!</td></tr><tr><td>. 2"!</td><td>. &==&+-Q=\$//=!2)1/019\$1+C!"8&1!</td></tr><tr><td>`TH!</td><td>`)/0+\$!)(!H1/\$1/!</td></tr><tr><td>`":FD!</td><td>`&/0)1&8!")88Q/0)1!:0=+-	\$!F80G01&/0)1!DC=/\$G!</td></tr><tr><td>`]d!</td><td>`\$%-\$8)G\$/#0+!]Q#B0'0/C!d10/=!</td></tr><tr><td>Tb.!</td><td>T08!&1 'S)#! b &U&# ') Q=! . &/\$#0&8=!</td></tr></tbody></table>

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:</td <td>./338</td> <td>./323</td> <td>./3.8</td> <td>./776</td> <td>./76.</td> <td>./433</td> <td>./426</td> <td>!"#%(</td> <td>!"##*</td> <td>!"&\$\$</td> <td>! "&+ '</td> <td>!"&)'</td> <td>!"*(%</td> <td>!"*##</td>	./338	./323	./3.8	./776	./76.	./433	./426	!"#%(!"##*	!"&\$\$! "&+ '	!"&)'	!"*(%	!"*##
=::	./32.	./702	./742	./788	./471	./462	!"#(%	<i>!"</i> #&&	!"&%\$!"&#(</td><td>! "& ! %</td><td>!"*()</td><td>!"*&(</td><td>!"*!'</td></tr><tr><td>=?:</td><td>./714</td><td>./754</td><td>./7.6</td><td>./441</td><td>./482</td><td>!"#'%</td><td>!"#[*]#</td><td>! "&% !</td><td>!"&&\$</td><td>!"&!!</td><td>!"*'&</td><td>!"*&!</td><td>!")\$\$</td><td>!")(*</td></tr><tr><td>>::</td><td>./727</td><td>./402</td><td>./450</td><td>./4.5</td><td><i>!"#</i>+\$</td><td>!"#)+</td><td>!"&(*</td><td>! "&& !</td><td>!"*\$*</td><td>!"*+'</td><td>!"**&</td><td><i>!")\$</i>&</td><td>!")'(</td><td><i>!")#</i>&</td></tr><tr><td>>?:</td><td>./415</td><td>./420</td><td>!"#\$#</td><td><i>!</i>"##\$</td><td>!"#!+</td><td>!"&'&</td><td>! "& * *</td><td>!"*%#</td><td>!"*#\$</td><td>!"*)(</td><td>!")%%</td><td>!") ' *</td><td>!")&\$</td><td>!"))%</td></tr><tr><td>?::</td><td>./42.</td><td>!"#%+</td><td>!"##!</td><td>!"&\$'</td><td>!"&+#</td><td>!"&)#</td><td>!"*('</td><td>!"*#*</td><td>!"*)!</td><td>!")%*</td><td>!")+'</td><td>!")&#</td><td>!"))+</td><td>!"!\$(</td></tr><tr><td>??:</td><td><i>!"#(</i>+</td><td>!"#&)</td><td>!"&%(</td><td><i>!</i> "&#+</td><td>!"&!'</td><td>!"*'\$</td><td>!"*&+</td><td>!"*!#</td><td>!")('</td><td>!")+*</td><td>!")&!</td><td>!")))</td><td><i>!"!\$</i>#</td><td>!"!%!</td></tr><tr><td>@::</td><td>!"#[*])</td><td>! "& (%</td><td>!"&& (</td><td>!"*\$%</td><td>!"*')</td><td>!"* *%</td><td>!")\$%</td><td>!")()</td><td>!")#(</td><td>!")*'</td><td>!")!(</td><td>!"!\$)</td><td>!"!((</td><td>!"!'+</td></tr><tr><td>@?:</td><td>!"&'\$</td><td>! "& *%</td><td>!"*\$!</td><td>!"*+#</td><td>!"**)</td><td>!")\$*</td><td>!") '+</td><td>!")#*</td><td>!")*)</td><td>!")!&</td><td>!"!%%</td><td>!"!(#</td><td>!"!'&</td><td><i>!"!</i>+&</td></tr><tr><td>A::</td><td><i>!</i> "& * <i>!</i></td><td>! " *% *</td><td>!"*#(</td><td>!"*)+</td><td>!")%'</td><td>!")'!</td><td>!")&(</td><td>!"))(</td><td>1")[]</td><td>!"!%+</td><td>!"!(*</td><td>!"!')</td><td>!"!+)</td><td><i>!"!#</i>&</td></tr><tr><td>היי¢/נ</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr></tbody></table>				

D".\$/E

	10/07/2002	10/07/2002	10/07/2002	10/08/2002	10/08/2002	10/08/2002	10/09/2002	10/10/2002	10/10/2002	10/11/2002
Chromium (total mg/L)				NA	NA	NA		NA	NA	
Copper (total mg/L)				NA	NA	NA		NA	NA	
Lead (total mg/L)				NA	NA	NA		NA	NA	
Silver (total mg/L)				NA	NA	NA		NA	NA	
Chromium (dissolved mg/L)	NA	NA	NA	NA	NA	NA		<0.01	<0.01	
Copper (dissolved mg/L)	NA	NA	NA	NA	NA	NA		<0.007	0.01	
Lead (dissolved mg/L)	NA	NA	NA	NA	NA	NA		<0.005	< 0.005	
Silver (dissolved mg/L)	NA	NA	NA	NA	NA	NA		<0.001	< 0.001	
VOCs (Laboratory)	NA	NA	NA	NA	NA	NA		NA	ND***	
Total Suspended Solids (mg/L)	NA	NA	NA	NA	NA	NA		NA	76	
Sheen	none	NA	none	none	NA	none		none	none	
Odor	organic	NA	none	slight organic	NA	none		organic	none	
Turbidity (NTU)	68.1	23	6	48.9	8.9	3		220	80	
Quicktest VOC (ppb)	NA	NA	0.0	NA	NA	0.0		NA	0.0	
Headspace (ppmV)	NA	NA	0.0	NA	NA	0.0		NA	0.0	
Volume Filtered (gal)	na	na	9,200	na	na	5,400		na	1,400	
Volume Bypassed (gal)	na	na	na	na	na	na		na	na	
Sheen	na	na	na	na	na	na		na	na	
Odor	na	na	na	na	na	na		na	na	
Turbidity (NTU)	na	na	na	na	na	na		na	na	
Headspace (ppmV)	na	na	na	na	na	na		na	na	

Notes:

NA = Not Analyzed na = not applicable

10/21/2002 10/22/2002 10/23/2002 10/23/2002

li	IT			1	1		[1
	10/28/2002	10/29/2002	10/29/2002	10/30/2002	10/31/2002	11/01/2002	11/02/2002	11/02/2002
Chromium (total mg/L)		NA	NA				NA	NA
Copper (total mg/L)		NA	NA				NA	NA
Lead (total mg/L)		NA	NA				NA	NA
Silver (total mg/L)		NA	NA				NA	NA
Chromium (dissolved mg/L)		<0.01	<0.01				NA	NA
Copper (dissolved mg/L)		< 0.007	0.009				NA	NA
Lead (dissolved mg/L)	JOS -	< 0.005	< 0.005	J.S.	J.S		NA	NA
Silver (dissolved mg/L)	. chron -	<0.001	<0.001	. Anor	. chiai		NA	NA
VOCs (Laboratory)	20-	NA	ND	20-	AD.		NA	NA
Total Suspended Solids (mg/L)	CHEFE	NA	53	CHERE	CHEFE	æ	NA	NA
Sheen	201	None	None	20	20	-thans	None	None
Odor	•	Slight Organic	Organic			, Olar	Organic	Slight Organic
Turbidity (NTU)		13.8	79			4	NA	NA
Quicktest VOC (ppb)		NA	0.0				NA	0.0
Headspace (ppmV)		NA	0.0				NA	NA
Volume Filtered (gal)		na	6,400				na	2,900
Volume Bypassed (gal)	15,800	na	33,300	18,300	15,800		na	29,700
Sheen	NR	na	NR	NR	none		na	none
Odor	NR	na	NR	NR	none		na	none
Turbidity (NTU)	NR	na	NR	NR	95		na	20
Headspace (ppmV)	NR	na	NR	NR	0.0		na	0.0

Notes:

NA = Not Analyzed

na = not applicable

INF = influent (prior to frac tank)

EFF = effluent (after 1 micron filter)

*Starting Day-7 10/10/02 the .5 Micron

filters were removed, therefore

no mid-point sampling was necessary.

*WEEK-5-INF and EFF = Designation for laboratory analytical samples

** No treated dewatering fluids were discharged, however, "surface water" was diverted to the wetlands. Diverted water

was screened for turbidity, sheen, and VOCs. No sheen or VOCs were detected via screening methods.

NR = No Reading

	11/17/2002	11/18/2002	11/19/2002	11/20/2002	11/21/2002	11/22/2002	11/23/2002	11/24/2002	11/25/2002
Chromium (total mg/L) Copper (total mg/L) Lead (total mg/L) Silver (total mg/L) Chromium (dissolved mg/L) Copper (dissolved mg/L) Lead (dissolved mg/L) Silver (dissolved mg/L) VOCs Total Suspended Solids (mg/ Sheen Odor Turbidity (NTU) Quicktest VOC (ppb) Headspace (ppmV) Volume Filtered (gal)	the Diedrates	Notiectage	No Diedrauge	No Fillered Discharge	No Fillered Die transe	No Diedense	No Diedrause	No Diedrauge	Notischarge
Volume Bypassed (gal)				NR	134,500				
Odor				none	none				
Turbidity (NTU) Headspace (ppm\/)				4	47 0.0				

Notes: NR = No Reading

	11/26/2002	11/26/2002	11/27/2002	11/28/2002	11/29/2002	11/30/2002	12/01/2002
Chromium (total mg/L)	NA	NA					
Copper (total mg/L)	NA	NA					

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